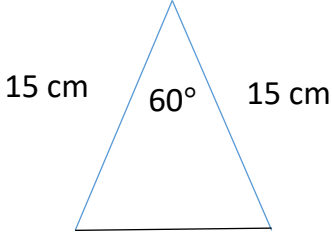
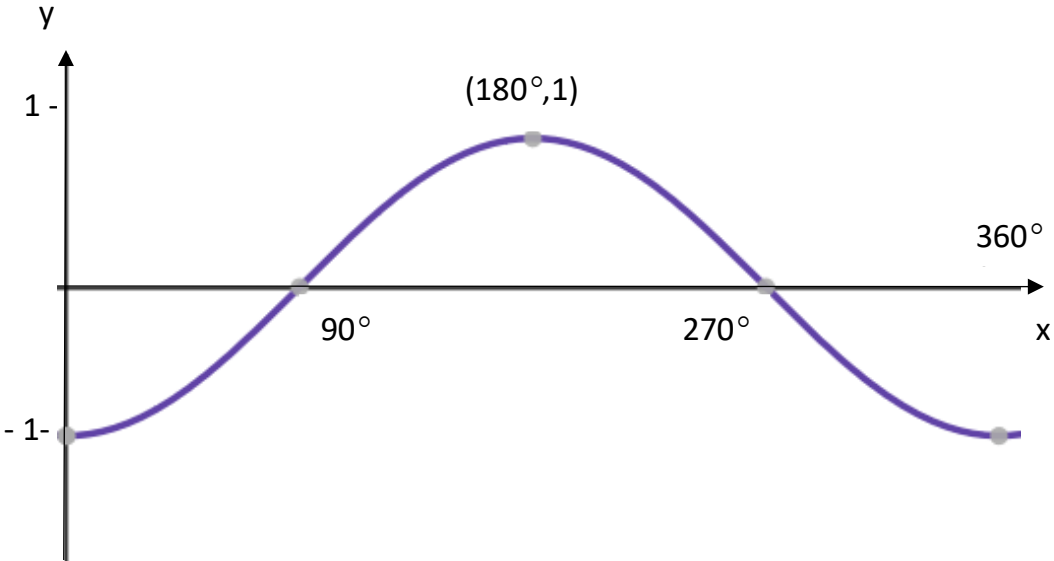


	Calculator Prelim Revision 4 - Answers	
1	Find the decimal multiplier	$100\% - 7\% = 93\% = 0.93$
	Use the formula for 3 years	$85\,500 \times 0.93^3$
	Give both unrounded and rounded answer	$68772.5236 = 68\,800 \text{ tonnes}$
	Full marks can also be awarded for finding the decrease year by year	
	2019	$85500 \times 0.93 = 79515$
	2020	$79515 \times 0.93 = 73948.92$
	2021	$73948.92 \times 0.93 = 68772.5235 \quad 68\,800 \text{ tonnes}$
	No marks will be given subtracting 7% 3 times $85\,500 - 3 \times 5985 = 67545$	
2	Substitute t into the formula and set equal to 88	$88 = 4 - 2t$
	Solve for t	$84 = -2t, \quad t = -42$
	No marks are given for substituting 88 into the formula $4 - 2 \times 88 = -172$	
3	Use the formula for the area of a sector	$A = \frac{\theta}{360} \times \pi \times r^2$
	Use $360^\circ - 110^\circ = 250^\circ$ for the angle	$A = \frac{250}{360} \times \pi \times 26^2$
	Give the answer with correct units	$A = 1474.8 \text{ cm}^2$
	2 marks are available for:	
	<ul style="list-style-type: none"> the area of the minor sector $A = \frac{110}{360} \times \pi \times 26^2 = 648.9 \text{ cm}^2$ The arc length of the major sector $Arc = \frac{250}{360} \times \pi \times 2 \times 26 = 113.4 \text{ cm}$ 	
4	Give your answer in scientific notation	$0.08 \times (3.6 \times 10^{-3}) = 0.000288 = 2.88 \times 10^{-4} \text{ grams}$

5	Mean is $\bar{x} = 154 \div 7 = 22\text{ }^{\circ}\text{C}$																																				
	<table><tr><th>x</th><th>x^2</th><th>$x - \bar{x}$</th><th>$(x - \bar{x})^2$</th></tr><tr><td>22</td><td>484</td><td>0</td><td>0</td></tr><tr><td>23</td><td>529</td><td>1</td><td>1</td></tr><tr><td>25</td><td>625</td><td>3</td><td>9</td></tr><tr><td>21</td><td>441</td><td>-1</td><td>1</td></tr><tr><td>19</td><td>361</td><td>-3</td><td>9</td></tr><tr><td>24</td><td>576</td><td>2</td><td>4</td></tr><tr><td>20</td><td>400</td><td>-2</td><td>4</td></tr><tr><td>$\Sigma 154$</td><td>$\Sigma 3416$</td><td>$\Sigma 0$</td><td>$\Sigma 28$</td></tr></table>	x	x^2	$x - \bar{x}$	$(x - \bar{x})^2$	22	484	0	0	23	529	1	1	25	625	3	9	21	441	-1	1	19	361	-3	9	24	576	2	4	20	400	-2	4	$\Sigma 154$	$\Sigma 3416$	$\Sigma 0$	$\Sigma 28$
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	Standard deviation is $\sqrt{\frac{3416 - \frac{154^2}{7}}{6}} \quad s = \sqrt{\frac{28}{6}} = 2.16\text{ }^{\circ}\text{C}$																																				
	The standard deviation is less than $2.3\text{ }^{\circ}\text{C}$, but the mean temperature is not within the given tolerance (22.04 to 23.06), so the system is not working effectively.																																				
6	(a) $V(\text{cone}) = \frac{1}{3}\pi \times 5^2 \times 6 = 157.079 = 157\text{cm}^3$ (b) Substitute into volume of a cylinder $157 = \pi \times 4^2 \times h$ Calculate the height of the cylinder $h = \frac{157}{16\pi} = 3.123V$, height is 3.1 cm																																				
7	Use the cosine rule $RT^2 = 14^2 + 16^2 - 2 \times 14 \times 16 \times \cos 43$ $RT^2 = 124.3535417 \dots$, $RT = 11.15\text{ cm}$																																				
8	Use 3D Pythagoras in one calculation or two Space diagonal is $\sqrt{7^2 + 4^2 + 5^2} = \sqrt{90} = 9.49\text{ cm}$ Base diagonal is $\sqrt{7^2 + 4^2} = \sqrt{65}$, Space diagonal is $\sqrt{(\sqrt{65})^2 + 5^2} = \sqrt{90} = 9.49\text{ cm}$ The 10 cm ruler will not fit into this box as $10\text{cm} > 9.49\text{ cm}$																																				
9	P and Q are the roots of the equation $x^2 - 6x + 5 = 0$ Factorise $(x - 1)(x - 5) = 0$ Solve $x = 1, x = 5$ State coordinates P (1,0), Q(5,0) The axis of symmetry lies halfway between these roots $x = 3$ No marks will be given for part (b) for axis of symmetry is 3																																				

10	<p>Use the area formula for 6 triangles with dimensions</p> <div style="display: flex; align-items: center; justify-content: space-around;"> <div style="text-align: center;">  <p>15 cm 60° 15 cm</p> </div> <div> $A(\text{one triangle}) = \frac{1}{2} \times 15 \times 15 \times \sin 60$ $= 97.4 \text{ cm}^2$ $\text{Area of table} = 6 \times 97.4 = 584.4 \text{ cm}^2$ </div> </div> <p>3 marks will be given for $A = 6 \times \frac{1}{2} \times 30 \times 30 \times \sin 60 = 2338.3 \text{ cm}^2$</p>
11	<p>Correct fraction $\left(\frac{3}{5}\right)^2 = \frac{9}{25}$, laws of indices $(p^4)^2 = p^4 \times 2$, $\left(\frac{3}{5}p^4\right)^2 = \frac{9}{25}p^8$</p>
12	<p>Substitute into the arc length formula $20 = \frac{65}{360} \times \pi \times D$ Calculate the diagonal $\frac{20 \times 360}{\pi \times 65} = D$, $D = 35.26 \text{ cm}$ Calculate the radius $r = 35.26 \div 2 = 17.63 \text{ cm}$</p> <p>2 marks will be given for use of area formula $20 = \frac{65}{360} \times \pi \times r^2$, $r = 5.9 \text{ cm}$</p>
13	<p>The height after 30 seconds is $h(30) = 10 + 6 \sin 30^\circ = \mathbf{13 \text{ m}}$ Form an equation $12 = 10 + \sin t$ Rearrange $\sin t = \frac{2}{6}$ First answer $t = 19.5^\circ$ Second answer $t = 160.5^\circ$</p>
14	<p>Minimum value at $(0^\circ, -1)$ and $(360^\circ, -1)$. Maximum value at $(180^\circ, 1)$ x-intercepts at $(90^\circ, 0)$ and $(270^\circ, 0)$, y-intercept at $(0^\circ, -1)$</p> <div style="text-align: center;">  </div>